



OPTIMAL DISTRIBUTED GENERATION PLACEMENT AND SIZING TO REDUCE ACTIVE POWER LOSS USING GA AND ACO ALGORITHM

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ABSTRACT

In this paper, Genetic Algorithm (GA) and Ant colony Algorithm (ACO) optimization techniques are proposed to find optimal sizing and location for distributed generation in electrical networks. The objective function of the work relies upon a linearized model to compute the active power losses as a function of power generators. This strategy based on a strong coupling between active power and power flow taking into consideration the voltage angles. With the end goal to exhibit the adequacy of the proposed method, the proposed strategy is applied on IEEE 30-bus standard systems. Different maximum penetration level capacity of DG units with three ranges such as, 10%, 20% and 30% of maximum power load and various possible places of DG units among several types of DG (active, reactive or active and reactive power) are considered. Results show that the optimization tools employing GA and ACO are effective in reducing active power losses and cost loss by finding the optimal placement and sizing of DG units.

Keywords: Genetic Algorithm; Distributed Generation; Planning Of DG; Optimum Allocation Of DG; Genetic Algorithm (GA); Ant Colony Algorithm (ACO).

المخلص :

يمكن دمج وحدات المولدات الموزعة DG في أنظمة التوزيع لتلبية الطلب المتزايد على الحمل، ويمكن استخدام DG لتحسين أنظمة توليد الطاقة وتحسين كفاءة نظام التوزيع، ومع ذلك يمكن أن يؤدي تركيب وحدات DG في مكان وتحميل غير ملائمين إلى تأثيرات سلبية مثل زيادة في فقد الطاقة وانتهكات قيود النظام، و نظراً للطلب المتزايد في قطاع الطاقة، هناك عدد كبير من المشكلات المتعلقة بإدارة قابلة للعديد من مشكلات نظام التوزيع مثل تنظيم الجهد وتقليل فقد الطاقة. يمكن خطوط نقل الكهرباء، ويعد وضع DG المناسب حالاً موثقاً أن يؤثر وضع (DG) في نظام التوزيع بشكل كبير على حالة التشغيل وديناميكيات أنظمة النقل والتوزيع. لذلك، من الضروري إتباع طريقة يمكنها تحديد موقع وحجم DG الأمثل.

الكلمات الدالة: الخوارزمية الجينية GA خوارزمية مستعمرة النمل ACO، المولدات الموزعة DG

الموقع الأمثل للمولدات الموزعة DG، لحجم الأمثل للمولدات الموزعة DG

APPRIVIATION LIST

DG	Distributed generator
GA	Genetic algorithm
ACO	Ant colony optimization
CSA	Cuckoo Search Algorithm
GSA	Gravitational Search Algorithm
PSO	Particle Swarm Optimization
PF _j	Power factor of bus j
P _{Loss}	Power loss
P _{DGj}	Active power of distributed generator at bus j
Q _{DGj}	Reactive power of distributed generator at bus
Pl	Active power load
<i>Of</i>	Objective function
f	Fitness function

I. INTRODUCTION

As the electrical energy demands develop yearly, extensive amount of capital cost expected to put in new power stations, also, development of transmission and distribution lines is an important issue. These sums can be lessened by utilizing distributed generators which can be strategically placed nearer to load centers. The siting and sizing of the distributed generation (DG) are the most difficult part for most utilities to be resolved. The increasing of the penetration level of distributed generation (DG) in electrical networks will reduction the power losses, develop the voltage profile and enhance security and stability of the power system. DG offers a huge number of environmental and financial benefits, and it compatibly guarantees a reasonable limit development in distribution systems with enhanced productivity and reliability. However, these points of interest can't be completely misused if inappropriate siting and sizing of DGs are determined. The integration of DG units into distribution networks, including sizing and placements, has pulled vast interest during the most recent 15 years.

The issue of choosing the optimal conductor for a real radial distribution system in Egypt is researched utilizing an ongoing meta-heuristic Algorithm, known as salp swarm enhancement [1]. An enhancement strategy dependent on the Genetic Algorithm (GA) related to the power flow (PF) technique is utilized to enhance the distribution network (DN) performance and to distinguish the best location and size of the DG's [2]. Studying analyses and addresses the effect of the integration of customer-owned DG on the arranging of active network management (ANM) plans and maximum DG penetration limits [3]. In [4], presenting a system to obtain the optimal location and sizing of DG units to highlight these advantages considering the load variation using genetic algorithm (GA) method. Comparison of optimal DG location applying CSA, GSA, PSO and GA for minimum real power loss in radial distribution system [5]. Reference [6] proposes a data-driven technique dependent on distributionally robust optimization to determine the maximum penetration level of distributed generation (DG) for active distribution networks (ADNs). Optimal location & Sizing of DG's using Backtracking Search Algorithm in IEEE 33-bus Distribution System [7]. In [8], proposing a novel methodology using the population depends on heuristic approach namely Particle Swarm Optimization (PSO) and New Particle Swarm Optimization (NPSO) for selecting the optimal sizing of Distributed Generator (DG) in the distribution systems. in [9], producing an optimization algorithm that employs modified flower pollination algorithm (MFPA) to select the optimal DGs allocation to minimize the system power losses, the performance of the proposed MFPA is investigated on three standard test systems; IEEE 33-bus, IEEE 69-bus and IEEE 136-bus. A real option valuation framework is proposed to choose the optimal investment strategies for DG including the investment location, size, and timing [10]. The optimal planning approach uses simulated annealing (SA) to select the optimal size and location of a mix of distributed generation (DG) candidate technologies to obtain required reliability criteria [11].

New hybrid method has been proposed for adding distributed generation with optimal power injections on power distribution systems to reduce power loss, this hybrid approach has been tested on IEEE 33-bus system and results are presented [12]. An efficient SPSO (Selective Particle Swarm Optimization) algorithm is presented to solve the optimal DG location problem in radial distribution systems; objective function is formulated for determining the optimal placement and sizing of distributed generation (DG) units in the distribution network for real power loss reduction and voltage profile improvement [13].

The locations of DGs are determined by using Index Vector Method (IVM) approach and Artificial Bee Colony (ABC) optimization algorithm has been employed to determine the optimum size, the proposed approach has been proved on standard 15-bus and 33-bus Radial Distribution Network (RDN) [14]. The distribution system reconfiguration (DSR), for considering network configuration impact that runs in offline mode with fixed loads, and optimal DG allocation and sizing issues are studied at the same time to find an optimal condition for distribution network depends on operational thresholds and reliability improvements, Non-dominated Sorting Genetic Algorithm is used to fix these problems simultaneously [15]. A Genetic Algorithm (GA) optimization method proposed to find optimal sizing and location of multi distributed generations in electrical networks, it is tested on (14, 30 and 57) IEEE standard systems [16]. Optimal distributed generation allocation using evolutionary algorithms in meshed network, the proposed method is applied on a standard IEEE 30-bus system with various DG penetration limits, the results received show the choice of the appropriate optimization algorithm and the effect of the constraints considered for optimal sizing and placement of the DGs [17]. In [18], presenting an analytical approach for optimal allocation and sizing of distributed generation (DG) in radial power Distribution networks to minimize active and reactive power losses, the proposed method is applied on 33-bus and 69-bus radial distribution test systems. In [19]. In this paper, optimization algorithms to calculate power losses has been developed to find optimal DG's sizing and siting depends on Genetic Algorithm (GA) and Ant Colony Algorithm (ACO). The genetic and ant colony algorithms offer significant advantages over many typical search of optimization technique ability to solve large-scale linear and nonlinear problems. The classification of this paper is as follows: section 2 gives brief information about GA and ACO. The formulation of methodology is given in section 3. Section 4 presents the case study on the IEEE-30 bus, test network. Finally, conclusions are summarized in section 5.

II. THE PROPOSED ALGORITHMS

A. GENETIC ALGORITHM

Optimization tools have great importance for optimal sizing and allocation of DG. GA is the most optimization tool used for solving this problem. GA is dependent on the natural selection and genetics [21]. It is a search based optimization algorithm and proper for solving the unconstrained optimization problems. To start the search steps, generate the initial population. The size of population should be determined and fixed pending the GA. In the second phase, the fitness function is estimated for given populations. Then, a new population it must be produced to find the optimal solution. There are three operators to estimated population of design vectors [21]; Propagation: This operator is used to determine the strings with the above-average fitness value from population and insert their multiple copies based on the probabilistic procedure.

Crossover: it should be implemented after the propagation. Its goal is to create new strings in the population by exchanging the information. Generally, two strings are selected randomly from the population and some portions of those are exchanged between selected strings. Mutation: After the crossover operation, the mutation operator must be applied to the new strings. The specific bits of the strings 0 to 1 or vice versa changed by this operator. Each generation consists of

propagation, crossover and mutation. Fig. 1 shows the flowchart of the proposed GA-based solution technique.

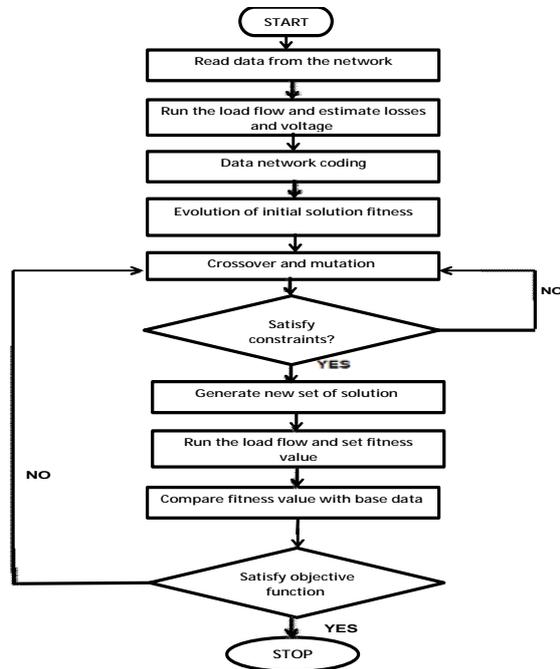


Fig.(1): GA technique flow chart

B. ANT COLONY ALGORITHM

1. General Aspects

The general ACO algorithm derived from the behavior of real ants is illustrated in Fig. 2. The procedure of the ACO algorithm manages the scheduling of three activities. The first step consists mainly in the initialization of the pheromone trail. In the iteration (second) step, each Ant constructs a complete solution to the problem according to a probabilistic state transition rule. The state transition rule depends mainly on the state of the pheromone. The third step updates quantity of pheromone; a pheromone updating rule is applied in two phases. First is an evaporation phase where a fraction of the pheromone evaporates, and then there is a reinforcement phase increasing amount of pheromone on path with high quality solutions. This process is iterated until a stopping criterion is reached.[20]

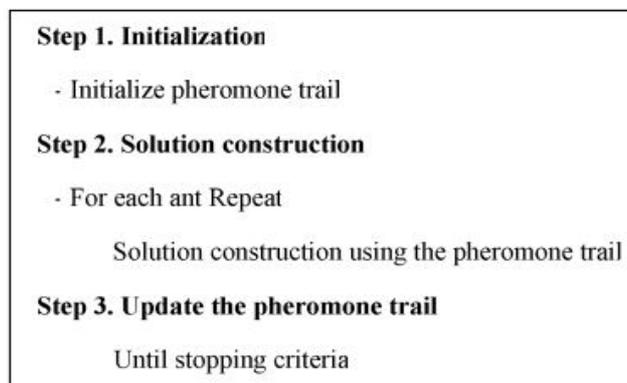


Fig. 2. A generic ACO algorithm.

Several different ways have been proposed to translate the above principles into a computational procedure to solve the optimization problem. The optimization approach proposed for in this paper is based on the ACO algorithm presented in [20], and outlined in the next subsection.

2. Applying ACO to DG Placement and sizing Problem

Applying ACO to DG Placement Problem Main steps of proposed ACO algorithm are listed below: Step1) Graph representation of search space First of all, we seek to devise a representation structure that is suitable for ants to search for solutions to the problem. The searching space of the problem is shown in Fig. 3.

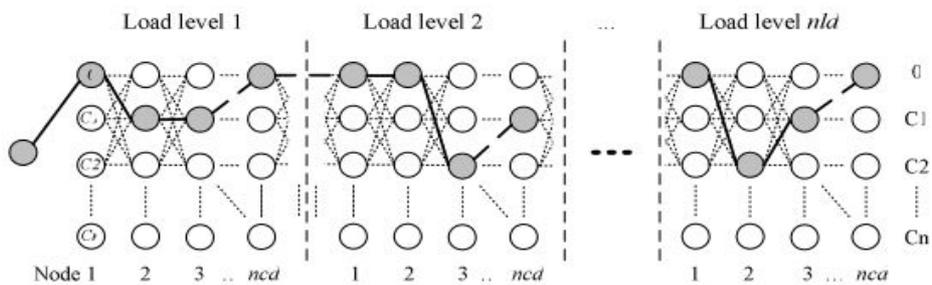


Fig. (3): Searching space of the problem.

All possible candidate capacity values in site n are represented by the states in the searching space in correspondence to stage n . The number of stages for each load level is equal to the number of candidate nodes of distribution system for DG placement. So, total number of stages is equal to $(nld \times ncd)$. A solution to the problem is produced after an ant completes its decision process for the sub-paths forming a tour.

Step2): ACO initialization in the beginning of ACO algorithm, the pheromone values of edges in search space are all initialized to a constant value $\tau_0 > 0$. This initialization causes ants choose their paths randomly and therefore, search the solution space more effectively.

Step3): Ant dispatch in this step, the ants are dispatched and solutions are constructed based on the level of pheromone on edges. Each ant will start its tour at the home colony and choose one of the states in the next stage to move according to following transition probability.

$$P_{ij}(t) = \frac{[\tau_{ij}(t)]}{\sum_{h \in \Delta_i} [\tau_{ij}(t)]}$$

Where, $\tau_{ij}(t)$ is the total pheromone deposited on edge ij at iteration t , and Δ_i represents the set of available edges which ant can choose at state i . After each ant ends its tour, a new solution for DG placement is generated which must be evaluated using fitness function.

Step4): Fitness function in this step, the fitness of tours generated by ants is assessed based on fitness function. The fitness function of the problem is defined as a penalty factor to the infeasible solutions (i.e., the ones violating the constraints). To speed up the convergence properties of algorithm and at the same time, to use the information that may still be useful in rejected tours, this penalty factor is linearly increased (through iterations) from zero toward a very high value.

Step5): Pheromone update the aim of the pheromone value update rule is to increase the pheromone values on solution components that have been found in high fitness solutions. Also, from a practical point of view, pheromone evaporation is needed to avoid a too rapid

convergence of the algorithm toward a sub-optimal region. It implements a useful form of forgetting, favoring the exploration of new areas in the search space. We use the following update rule in our study:

$$\tau_{ij}(t+1) = \begin{cases} \max\left\{(1-\rho)\tau_{ij}(t) + Q \cdot F(\Omega_B(t)), \tau_{\min}(t)\right\} \\ \text{if } (i, j) \in \Omega_B(t), \\ \max\left\{(1-\rho)\tau_{ij}(t), \tau_{\min}(t)\right\} \\ \text{otherwise,} \end{cases}$$

Where, $0 < \rho < 1$ is pheromone evaporation rate. $\Omega_B(t)$ is the best tour found until the end of iteration t , which is stored in a specific list variable and replaced each time some ant finds a tour with better quality function value. $F(\Omega_B(t))$ is the quality function value corresponding to $\Omega_B(t)$. Q is a heuristic variable which control amount of pheromone addition on the best tour. $\tau_{\min}(t)$ is lower bound of pheromone which results in a small probability for an ant to choose a certain edge; still the probability will be greater than zero. This lower bound is a function of the iteration counter as below:

$$\tau_{\min}(t) = \tau_{\min} \left(1 - \frac{t}{t_{\max}}\right)$$

Where, τ_{\min} is initial lower bound of pheromone.

Step6) Convergence determination the steps 3-5 continue until the iteration counter reaches the predefined maximum number which determines experimentally. The best tour selected among all iterations implies the optimal DG placement solution. Fig. 4 shows the flowchart of the proposed ACO-based solution technique [20].

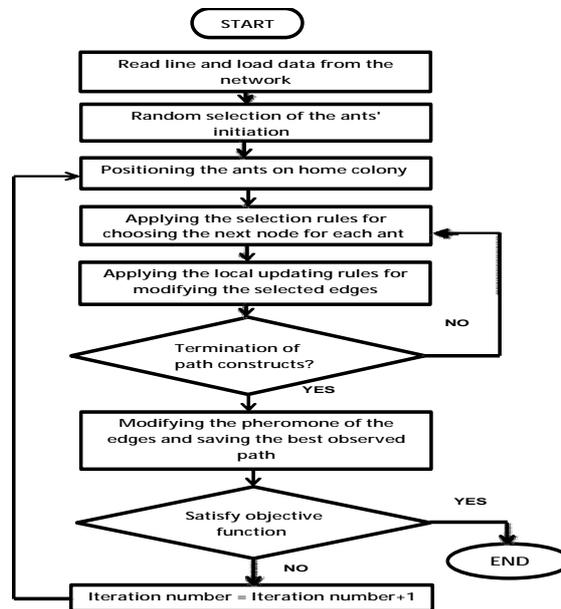


Fig. (4): Flowchart of the proposed ACO-based solution algorithm

III. PROBLEM FORMULATION

The main aim of this paper is to study the reliable performance of the system after placing the DG optimally at a suitable site. Since the purpose of DG is to decrease the total active power loss and improving the voltage profile, the installation of DG units at non-optimal places may not give accurate results which will be useful for improving the

system performance. However the losses cannot be totally removed, but they can be pushed down to an acceptable value. Since the impact of distributed generation on system performance based on system operating conditions and the type of the distributed generation, it is important to use some solutions in planning and operation to reach solutions for the best performance. The first objective is to decrease the total real power loss in the power system accounting DG which expressed as follows [5]:

Minimization of

$$f = \sum_{i=1}^N P_{Loss_i} \quad (1)$$

$$P_{Loss_i} = |I_i|^2 R_i \quad (2)$$

(2)

Where I_i is the current of branch i , and R_i is the resistance of branch i

With DG Subject to real power constraints given by:

$$\sum_{j=1}^N P_{DGj} = \sum_{j=1}^N P_{Dj} + \sum_{i=1}^N P_{Loss_i} \quad (3)$$

The inequality constraints on P_{DGj} of DG given by:

$$P_{DGj}^{min} \leq P_{DGj} \leq P_{DGj}^{max} \quad (4)$$

The inequality constraints on Q_{DGj} of DG given by:

$$Q_{DGj}^{min} \leq Q_{DGj} \leq Q_{DGj}^{max} \quad (5)$$

The equality constraints on P_{DGj} and Q_{DGj} of DG with constant power factor given by:

$$P.F_j = \cos \theta_j \quad (6)$$

$$\tan^{-1} \theta_j = \frac{Q_{Lj}}{P_{Lj}} \quad (7)$$

The Q_{DGj} given by:

$$Q_{DGj} = \tan^{-1} \theta_j \times P_{DGj} \quad (8)$$

where f is the total loss of the system, P_{Loss_i} is the real power loss at branch i , P_{Gj} is the active power generation at bus J , P_{DGj} is the total power demand, P_{Dj} is the total power demand, P_{DGj} is the real power generation for distributed generators, Q_{DGj} is the reactive power generation for distributed generator, P_{DGjmin} and P_{DGjmax} are the minimum and maximum active power generation limits at bus i for DG values, Q_{DGjmin} and Q_{DGjmax} are the minimum and maximum reactive power generation limits at bus i for DG values, $P.F_j$ is the power factor of bus i , P_{Lj} is the active power load at bus i , Q_{Lj} is the reactive

power load at bus j P_j , the angle between P_L and Q_L at bus j , and N is the total number of buses in the system. The second objective is directed towards the improvement in voltage profile of the bus system represented by the objective function (O_f) governed by the relation (9):

$$O_f = 1 - \sum_{i=1}^N v(i) \quad (9)$$

Here O_f = Objective Function in terms of voltages of all the buses and $v(i)$ is the voltage at bus i in the system. The GA and ACO algorithms are used for the optimal sizing of the DG's taking the minimum system losses as the constraint. The optimization algorithm runs until there is no more reduction in system losses taking in to account that the constraints are obeyed, the power loss reduction and cost loss reduction expressed as the followings equations:

$$P_{LossR} = \frac{\sum(P_{Loss})_{noDG} - \sum(P_{Loss})_{withDG}}{\sum(P_{Loss})_{noDG}} \times 100 \quad (10)$$

$$C_{Loss} = T \times \sum P_{Loss} \quad (11)$$

$$C_{LossR} = \frac{\sum(C_{Loss})_{noDG} - \sum(C_{Loss})_{withDG}}{\sum(C_{Loss})_{noDG}} \times 100 \quad (12)$$

P_{LossR} : active power loss reduction

$(P_{Loss})_{noDG}$: the power loss with out adding distributed generators

$(P_{Loss})_{withDG}$: the power loss with adding distributed generators

C_{Loss} : the cost of total power loss

T : the tariff per 1 MW

IV. CASE STUDY AND RESULTS

The proposed optimization technique has been simulated in MATLAB environment and tested for distribution systems. To verify the effectiveness and efficiency of the GA and ACO techniques, they have been applied to IEEE 30-bus system, which has its schematic diagram and all data shown in fig.5, table 1, table 2 and table 3. In this paper, minimization of the active power loss, cost of active power loss -and enhancement in the voltage profile are considered as objective functions. The proposed method is applied to an IEEE 30-bus system with the total active load of 283.4 MW and reactive load of 126.2 MVAR. The real power loss is 18.744 MW when calculated using load flow for the base case, bus one selected as slack bus, from economical case we assume 1000 LE is the tariff per 1 MW power loss.

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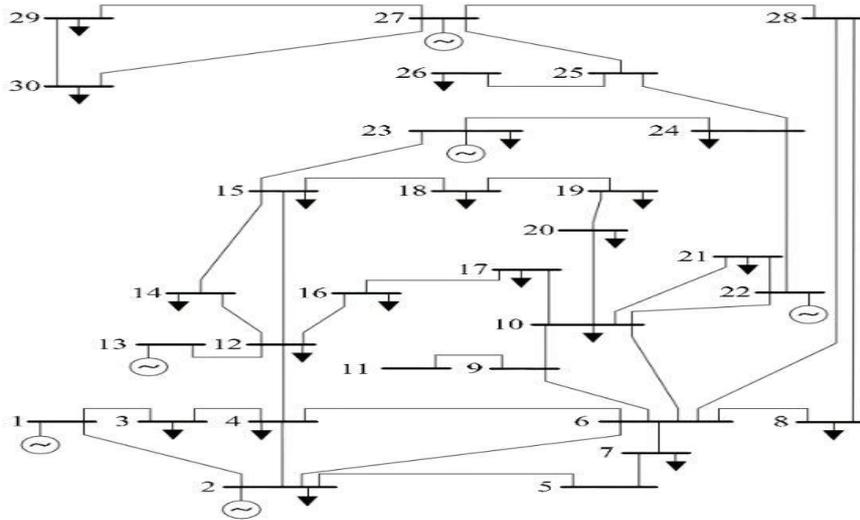


Fig. (5): schematic diagram of IEEE 30- bus system

Table (1): line data of IEEE 30-bus system

Line number	From Bus	To Bus	Line impedance (p.u.)		Half line charging susceptance (p.u.)	MVA Rating	Transformer Tap setting value (p.u.)
			Resistance	Reactance			
1	1	2	0.2	0.06	0.02	130	1
2	1	3	0.05	0.2	0.02	130	1
3	2	4	0.06	0.2	0.02	65	1
4	2	5	0.05	0.2	0.021	130	1
5	2	6	0.06	0.2	0.02	65	1
6	3	4	0.0132	0.04	0.0042	130	1
7	4	6	0.012	0.0414	0.005	90	1
8	4	12	0	0.3	0	65	0.932
9	5	7	0.05	0.12	0.01	70	1
10	6	7	0.03	0.082	0.009	130	1
11	6	8	0.012	0.042	0.0045	32	1
12	6	9	0	0.208	0	65	0.978
13	6	10	0	0.556	0	32	0.969
14	6	28	0.0169	0.0599	0.065	32	1
15	8	28	0.0636	0.2	0.0214	32	1
16	9	11	0	0.208	0	65	1
17	9	10	0	0.11	0	65	1
18	10	20	0.0936	0.209	0	32	1
19	10	17	0.0324	0.0845	0	32	1
20	10	21	0.0348	0.0749	0	32	1
21	10	22	0.0727	0.1499	0	32	1
22	12	13	0	0.14	0	65	1
23	12	14	0.1231	0.2559	0	65	1
24	12	15	0.0662	0.1304	0	32	1
25	12	16	0.0945	0.1997	0	32	1
26	14	15	0.221	0.1997	0	16	1
27	15	18	0.1073	0.2185	0	16	1
28	15	23	0.1	0.202	0	16	1
29	16	17	0.0824	0.1923	0	16	1
30	18	19	0.0639	0.1292	0	16	1
31	19	20	0.034	0.068	0	32	1
32	21	23	0.0116	0.0236	0	32	1
33	22	24	0.115	0.179	0	16	1
34	23	24	0.132	0.27	0	16	1
35	24	25	0.1885	0.3292	0	16	1
36	25	26	0.2544	0.38	0	16	1
37	25	27	0.1093	0.2087	0	16	1
38	27	29	0.2198	0.4153	0	16	1
39	27	30	0.24	0.58	0	16	1
40	28	27	0	0.396	0	65	0.968
41	29	30	0.13	0.4	0	16	1

Table (2): bus voltage and load and generation of IEEE 30-bus system

Bus Number	Bus Voltage		Generation		Load	
	Magnitude (p.u)	Phase Angle (Degree)	P (MW)	Q (MVAR)	P (MW)	Q (MVAR)
1	1.06	0	0	0	0	0
2	1	0	40	50	21.7	12.7
3	1	0	0	0	2.4	1.2
4	1	0	0	0	7.6	1.6
5	1	0	0	37	94.2	19
6	1	0	0	0	0	0
7	1	0	0	0	22.8	10.9
8	1	0	0	37.3	30	30
9	1	0	0	0	0	0
10	1	0	0	19	5.8	2
11	1	0	0	16.2	0	0
12	1	0	0	0	11.2	7.5
13	1	0	0	10.6	0	0
14	1	0	0	0	6.2	1.6
15	1	0	0	0	8.2	2.5
16	1	0	0	0	3.9	1.8
17	1	0	0	0	9	5.8
18	1	0	0	0	3.2	0.9
19	1	0	0	0	9.5	3.4
20	1	0	0	0	2.2	0.7
21	1	0	0	0	17.5	11.2
22	1	0	0	0	0	0
23	1	0	0	0	3.2	1.6
24	1	0	0	4.3	8.7	6.7
25	1	0	0	0	0	0
26	1	0	0	0	3.5	2.3
27	1	0	0	0	0	0
28	1	0	0	0	0	0
29	1	0	0	0	2.4	0.9
30	1	0	0	0	10.6	1.9

Table (3): generators data of IEEE 30-bus system

Generator Number	BUS Number	(MW)	(MVAR)
G1	1	0	80
G2	2	0	80
G3	13	0	50
G4	22	0	55
G5	23	0	30
G6	27	0	40

Case 1: 10% Penetration Level

The proposed methods are applied to IEEE 30-bus system with 10% of load penetration level, 10% of active power and reactive power load are 28.34 MW and 12.62 MVAR. Table 4 represents the comparison of active power loss, cost of active power loss and the percentage of power and cost loss reduction without DGs and with adding active power DGs, reactive power DGs and active reactive power DGs with constant power factor of bus with respect to its load, using GA and ACO. Fig.4 represents the comparison of average voltage profile of IEEE 30-bus without DGs and with implementing active power DGs, reactive power DGs and active reactive power DGs with constant power factor of bus with respect to its load using GA and ACO. For this case, two active power DG units are optimally sized and placed using ACO technique; the size and location of each DG are given in Table I. show that in fig.6 and table 5 the bus voltage profile, three active and reactive power DG units are optimally sized and placed using GA technique, the size and location of each DG and cost of power loss are given in table 4.

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Table (4): DG placement and sizing and cost of power loss by GA and ACO for IEEE 30-bus system (case1)

DG NUMBER	Techniques	DG Types	Implemented DG Schedule				DGs (MW)	DGs (MVAR)	Ploss (MW)	Cost Loss (LE)	Cost&P Loss Reduction (%)
NO DG								18.744	18744	0	
2DG	GA	P	BUS	5	15		28.342	0.0	14.661	14661	21.8
			Size (MW)	28.34	0.002						
		Q	BUS	4	2		0.0	12.7	18.269	18269	2.534
			Size (MVAR)	3.1	9.6						
		P & Q	BUS	24	17		28.34	20.243	14.55	14550	22.4
			Size (MW)	15.72	12.62						
		Size (MVAR)	12.11	8.133							
	ACO	P	BUS	5	30		28.34	0.0	14.531	14531	22.5
			Size (MW)	20	8.34						
Q		BUS	21	26		0.0	12.62	18.448	18448	1.6	
		Size (MVAR)	10	2.62							
P & Q		BUS	21	24		28.4	20.04	14.412	14412	23.11	
		Size (MW)	14.2	14.2							
	Size (MVAR)	9.1	10.94								
3DG	GA	P	BUS	5	5	7	28.4	0.0	14.646	14646	21.9
			Size (MW)	19.8	2.13	6.44					
		Q	BUS	2	26	12	0.0	12.7	18.254	18254	2.61
			Size (MVAR)	10.1	2.4	0.2					
		P & Q	BUS	5	19	19	28.4	6.8	14.582	14582	22.2
			Size (MW)	21.55	2.912	3.9					
		Size (MVAR)	4.35	1.04	1.4						
	ACO	P	BUS	5	30	30	28.4	0.0	14.524	14524	22.514
			Size (MW)	20	4.2	4.2					
		Q	BUS	23	26	30	0.0	12.62	18.448	18448	1.6
Size (MVAR)			10	1.31	1.31						
P & Q		BUS	24	21	30	28.4	15.1	14.607	14607	22.1	
		Size (MW)	9.45	9.45	9.45						
	Size (MVAR)	7.3	6.05	1.7							

Table 5: bus voltage profile (case 1)

Bus Number	Base Case	Genetic Technique						Ant Colony Technique					
		2DG Units			3DG Units			2DG Units			3DG Units		
		P	Q	P&Q	P	Q	P&Q	P	Q	P&Q	P	Q	P&Q
1	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06
2	1.01	1.01	1.02	1.02	1.01	1.02	1.01	1.01	1.01	1.02	1.01	1.01	1.01
3	0.99	0.99	1.00	1.01	0.99	0.99	0.99	0.99	0.99	1.01	0.99	0.99	1.00
4	0.98	0.98	0.99	0.99	0.98	0.98	0.98	0.98	0.98	0.99	0.98	0.98	0.99
5	0.97	0.99	0.98	0.98	0.98	0.98	0.98	0.98	0.98	0.98	0.98	0.98	0.98
6	0.97	0.96	0.96	0.99	0.98	0.98	0.96	0.96	0.98	0.99	0.98	0.98	0.99
7	0.96	0.98	0.97	0.98	0.97	0.97	0.98	0.97	0.97	0.98	0.97	0.97	0.98
8	0.97	0.98	0.98	0.99	0.98	0.98	0.98	0.98	0.98	0.98	0.98	0.98	0.98
9	0.99	0.99	0.99	1.02	0.99	0.99	0.99	0.99	1.00	1.02	0.99	1.00	1.00
10	0.99	0.99	0.99	1.02	0.99	0.99	0.99	0.99	1.00	1.02	0.99	1.00	1.01
11	1.00	1.00	1.00	1.01	1.00	1.00	1.00	1.00	1.00	1.01	1.00	1.00	1.00
12	0.99	1.00	1.00	1.02	1.00	1.00	1.00	1.00	1.01	1.02	1.00	1.01	1.01
13	1.00	1.00	1.00	1.02	1.00	1.00	1.00	1.00	1.01	1.02	1.00	1.01	1.01
14	0.98	0.99	0.99	1.01	0.99	0.99	0.98	0.99	0.99	1.01	0.99	0.99	1.00
15	0.97	0.98	0.98	1.01	0.98	0.98	0.98	0.98	0.99	1.01	0.98	0.99	1.00
16	0.98	0.99	0.98	1.02	0.98	0.98	0.98	0.98	0.99	1.02	0.98	0.99	1.01
17	0.98	0.98	0.99	1.03	0.98	0.99	0.99	0.99	0.99	1.02	0.98	0.99	1.00
18	0.97	0.97	0.97	1.00	0.97	0.97	0.98	0.97	0.98	1.01	0.97	0.98	0.99
19	0.97	0.97	0.97	1.00	0.97	0.97	0.98	0.97	0.98	1.00	0.97	0.98	0.99
20	0.97	0.97	0.98	1.01	0.97	0.98	0.98	0.97	0.99	1.01	0.97	0.99	0.99
21	0.97	0.98	0.98	1.01	0.98	0.98	0.98	0.98	0.99	1.02	0.98	0.99	1.00
22	0.98	0.98	0.98	1.03	0.98	0.98	0.98	0.98	0.99	1.03	0.98	0.99	1.01
23	0.97	0.98	0.98	1.01	0.98	0.98	0.99	0.97	0.99	1.02	0.98	0.99	1.00
24	0.97	0.97	0.97	1.03	0.97	0.98	0.98	0.97	0.99	1.03	0.97	0.99	1.01
25	0.97	0.97	0.98	1.01	0.97	0.98	0.98	0.98	0.99	1.02	0.98	0.99	1.01
26	0.95	0.96	0.96	0.99	0.96	0.97	0.96	0.96	0.98	0.99	0.96	0.98	0.99
27	0.98	0.99	0.99	1.01	0.98	0.99	0.99	0.99	0.99	1.01	0.99	0.99	1.02
28	0.97	0.98	0.98	0.99	0.98	0.98	0.98	0.98	0.98	0.99	0.98	0.98	0.99
29	0.96	0.97	0.97	0.99	0.97	0.97	0.97	0.98	0.98	0.99	0.98	0.98	1.01
30	0.95	0.96	0.96	0.99	0.96	0.97	0.96	0.96	0.97	0.98	0.96	0.98	1.01

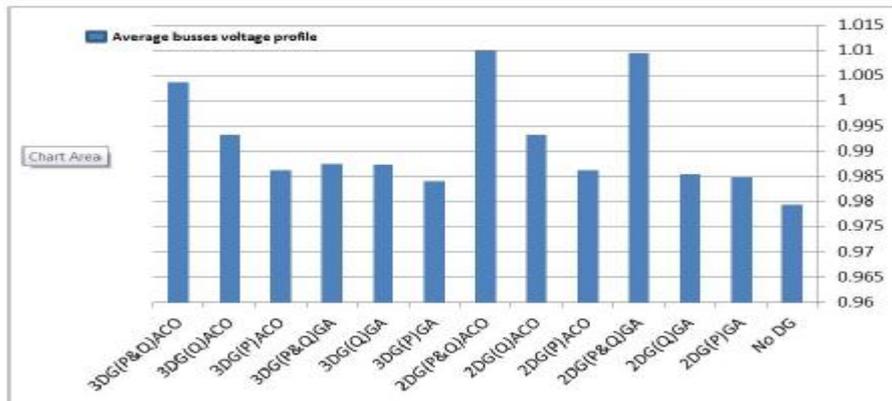


Fig. (5): Average voltages profile of IEEE 30- bus system (case1)

Case 2: 20% Penetration Level

The proposed methods are applied to IEEE 30-bus system with 20% of load penetration level, 20% of active power and reactive power load are 56.68 MW and 25.24 MVAR. Table 6 represents the comparison of active power loss, cost of active power loss and the percentage of power and cost loss reduction without DGs and with adding active power DGs, reactive power DGs and active reactive power DGs with constant power factor of bus with respect to its load, using GA and ACO. Figure 7 represents the comparison of average voltage profile of IEEE 30-bus without DGs and with implementing active power DGs, reactive power DGs and active reactive power DGs with constant power factor of bus with respect to its load, using GA and ACO. For this case, two active power DG units are optimally sized and placed using ACO technique; the size and location of each DG are given in Table 2. Show that in fig. 5 and table 7 the bus voltage profile, three active and reactive power DG units are optimally sized and placed using ACO technique, the size and location of each DG and cost of power loss are given table 6.

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Table (6): DG placement and sizing and cost of power loss by GA and ACO for IEEE 30-bus system (case2)

DG NUMBER	Techniques	DG Types	Implemented DG Schedule			DGs (MW)	DGs (MVAR)	Ploss (MW)	Cost Loss (LE)	Cost&P Loss Reduction (%)		
NO DG								18.744	18744	0		
2DG	GA	P	BUS	5	19							
			Siz (MW)	37.81	18.9		56.71	0.0	11.054	11054	41.12	
			Siz (MVAR)	2	21							
		Q	Siz (MW)	12.3	13		0.0	25.3	18.128	18128	3.2	
			Siz (MVAR)	5	21							
			Siz (MW)	26.74	29.94		56.7	24.6	10.908	10908	41.81	
	ACO	P	BUS	5	30							
			Siz (MW)	50	6.68		56.68	0.0	10.989	10989	41.4	
			Siz (MVAR)	21	2							
		Q	BUS	5	29							
			Siz (MW)	12.62	12.62		0.0	25.24	18.13	18130	3.3	
			Siz (MVAR)	5	29							
P & Q	Siz (MW)	40	16.68		56.68	16.44	10.872	10872	42			
	Siz (MVAR)	8.1	8.34									
	Siz (MW)	8.1	8.34									
3DG	GA	P	BUS	5	19	24						
			Siz (MW)	41.7	8.7	6.4	56.8	0.0	10.908	10908	41.81	
			Siz (MVAR)	2	21	19						
		Q	Siz (MW)	8.4	10.2	6.7	0.0	25.3	18.083	18083	3.5	
			Siz (MVAR)	5	21	7						
			Siz (MW)	36.7	14.1	5.93	56.73	19.3	10.779	10779	42.5	
	P & Q	Siz (MVAR)	7.4	8.024	2.835							
		Siz (MVAR)	5	30	21							
		Siz (MW)	30	6.68	20	56.7	0.0	10.905	10905	41.82		
	ACO	P	BUS	4	29	2						
			Siz (MW)	8.4	8.41	8.41	0.0	25.23	18.086	18086	3.5	
			Siz (MVAR)	21	30	5						
P & Q		Siz (MW)	30	6.68	20	56.7	24.43	10.807	10807	42.344		
		Siz (MVAR)	19.2	1.2	4.03							
		Siz (MVAR)										

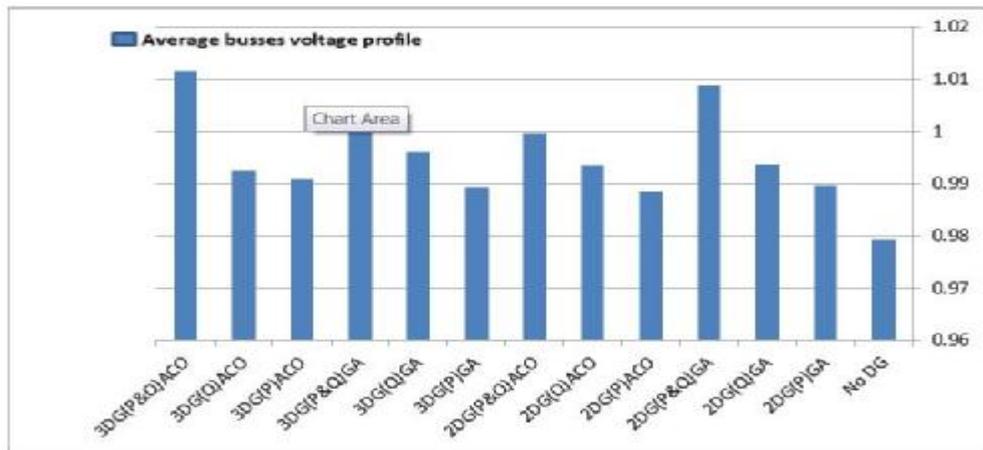


Fig. (7): Average voltages profile of IEEE 30- bus system (case2)

Table (7): bus voltage profile (case 2)

Bus Number	Base Case	Genetic Technique						Ant Colony Technique					
		2DG Units			3DG Units			2DG Units			3DG Units		
		P	Q	P&Q	P	Q	P&Q	P	Q	P&Q	P	Q	P&Q
1	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06
2	1.01	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02
3	0.99	1.00	1	1	1.01	1	1	1.01	1	1	1.01	1	1
4	0.98	0.99	0.99	0.99	1	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99
5	0.97	0.99	0.99	0.98	0.99	0.99	0.98	1	0.99	0.98	1	0.99	0.98
6	0.97	0.98	0.98	0.98	0.99	0.98	0.98	0.99	0.98	0.98	0.99	0.98	0.98
7	0.98	0.98	0.98	0.97	0.98	0.98	0.97	0.99	0.98	0.97	0.99	0.98	0.97
8	0.97	0.98	0.98	0.98	0.99	0.98	0.98	0.99	0.98	0.98	0.99	0.98	0.98
9	0.99	1.00	1	1	1.02	1	1	1.01	1	1	1.01	1	1
10	0.99	1.00	1	1.01	1.03	0.99	1.01	1.01	1	1.01	1.01	1	1
11	1.00	1.00	1	1	1.01	1	1	1	1	1	1	1	1
12	0.99	1.00	1	1.01	1.03	1	1.01	1.01	1	1.01	1.01	1	1.01
13	1.00	1.00	1	1.01	1.02	1	1.01	1.01	1	1.01	1.01	1	1.01
14	0.98	0.99	0.99	1	1.01	0.99	1	1	0.99	1	1	0.99	1
15	0.97	0.99	0.99	1	1.02	0.98	1	1	0.99	1	1	0.99	0.99
16	0.98	0.99	0.99	1	1.02	0.99	1	1	0.99	1	1.01	0.99	1
17	0.98	0.99	0.99	1	1.02	0.99	1	1	0.99	1	1	0.99	1
18	0.97	0.99	0.99	0.99	1.01	0.97	0.99	0.99	0.98	1	0.99	0.98	0.98
19	0.97	0.98	0.98	0.98	1	0.97	0.98	0.99	0.98	1	0.99	0.98	0.98
20	0.97	0.99	0.99	0.99	1.01	0.98	0.99	0.99	0.98	1	0.99	0.98	0.99
21	0.97	0.98	0.98	1	1.03	0.98	1	1	0.98	1	1	0.99	0.99
22	0.98	0.99	0.99	1	1.02	0.99	1	1	0.99	1	1	0.99	0.99
23	0.97	0.98	0.98	1	1.02	0.98	0.99	1	0.98	1	1	0.99	0.99
24	0.97	0.98	0.98	0.99	1.01	0.98	0.99	0.99	0.98	0.99	0.99	0.98	0.98
25	0.97	0.98	0.98	0.99	1	0.98	0.99	0.99	0.98	0.99	0.99	0.98	0.98
26	0.95	0.96	0.96	0.97	0.98	0.96	0.97	0.97	0.96	0.97	0.97	0.97	0.97
27	0.98	0.99	0.99	0.99	1.01	0.99	0.99	1	0.99	0.99	1	0.99	0.99
28	0.97	0.98	0.98	0.98	0.99	0.98	0.98	0.99	0.98	0.98	0.99	0.98	0.98
29	0.98	0.97	0.97	0.97	0.99	0.98	0.97	0.98	0.97	0.97	0.98	0.98	0.97
30	0.95	0.96	0.96	0.97	0.98	0.96	0.97	0.97	0.96	0.97	0.97	0.98	0.97

Case 3: 30% Penetration Level

The proposed methods are applied to IEEE 30-bus system with 30% of load penetration level, 30% of active power and reactive power load are 85.02 MW and 37.86 MVAR. Table 8 represents the comparison of active power loss, cost of active power loss and the percentage of power and cost loss reduction without DGs and with adding active power DGs, reactive power DGs and active reactive power DGs with constant power factor of bus with respect to its load, using GA and ACO. Figure 8 represents the comparison of average voltage profile of IEEE 30-bus without DGs and with implementing active power DGs, reactive power DGs and active reactive power DGs with constant power factor of bus with respect to its load, using GA and ACO. For this case, three active and reactive power DG units are optimally sized and placed using ACO technique; the size and location of each DG are given in Table III. Show that in fig.6 the best solution for maximum average voltage profile is; two active and reactive power DG units are optimally sized and placed using ACO technique; the size and location of each DG are given in table 8.

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Table (8): DG placement and sizing and cost of power loss by GA and ACO for IEEE 30-bus system (case3)

DG NUMBER	Techniques	DG Types	Implemented DG Schedule			DGs (MW)	DGs (MVAR)	Ploss (MW)	Cost Loss (LE)	Cost&P Loss Reduction (%)	
NO DG								18.744	18744	0	
2DG	GA	P	BUS	5	21	85.1	0.0	8.392	8392	55.23	
			Size (MW)	49.25	35.8						
		Q	BUS	3	4	0.0	37.51	17.958	17958	4.2	
			Size (MVAR)	3.4	34.11						
		P & Q	BUS	5	8	85.04	41.02	8.397	8397	55.22	
			Size (MW)	55.14	29.9						
	ACO	P	BUS	5	19	85.02	0.0	8.527	8527	54.51	
			Size (MW)	70	15.02						
		Q	BUS	2	21	0.0	37.9	18.109	18109	3.4	
			Size (MVAR)	18.93	18.93						
P & Q	BUS	5	21	85.02	23.733	8.326	8326	55.6			
	Size (MW)	70	15.02								
Size (MVAR)	14.12	9.613									
	3DG	GA	P	BUS	5	8	14	84.7	0.0	8.701	8701
Size (MW)				72.2	9.1	3.4					
Q			BUS	2	15	21	0.0	37.93	18.039	18039	3.8
			Size (MVAR)	10.1	9.7	18.13					
P & Q			BUS	5	15	19	85.07	21.24	8.257	8257	55.95
			Size (MW)	55.9	10.94	18.83					
Size (MVAR)		11.3	3.2	6.74							
		ACO	P	BUS	5	19	30	85.02	0.0	8.353	8353
Size (MW)				70	8	7.02					
Q			BUS	4	22	2	0.0	35.95	17.994	17994	4
	Size (MVAR)		20	8.85	7.1						
P & Q	BUS		23	5	30	85.05	28.3	8.197	8197	56.3	
	Size (MW)		40	40	5.05						
Size (MVAR)	20	8.1	0.2								

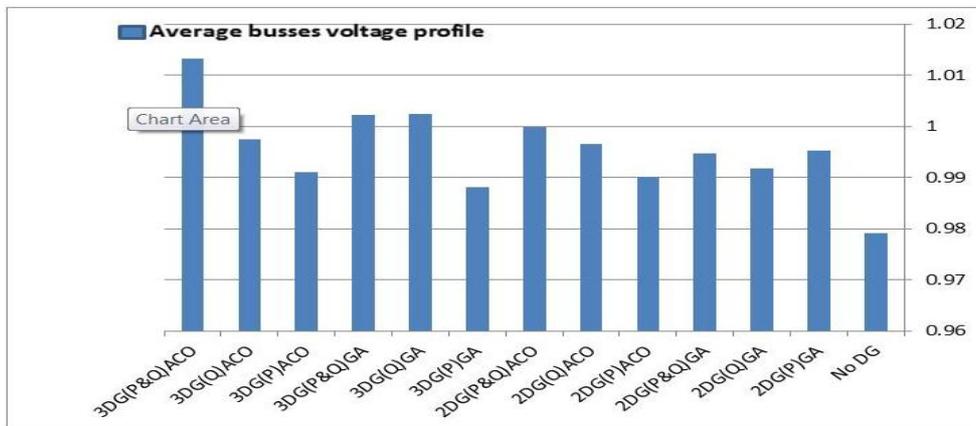


Fig. (8): Average voltages profile of IEEE 30- bus system (case2)

Table (9): bus voltage profile (case 3)

Bus Number	Base Case	Genetic Technique						Ant Colony Technique					
		2DG Units			3DG Units			2DG Units			3DG Units		
		P	Q	P&Q	P	Q	P&Q	P	Q	P&Q	P	Q	P&Q
1	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06	1.06
2	1.01	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02	1.02
3	0.99	1.01	1.01	1.01	1	1	1.01	1	1	1.01	1	1.01	1.01
4	0.98	0.99	1	0.99	0.99	0.99	0.99	0.99	0.99	1	0.99	1	1
5	0.97	1	0.98	1	1	0.98	1	1	0.98	1	1	0.98	1
6	0.97	0.99	0.99	0.99	0.98	0.98	0.99	0.98	0.98	0.99	0.98	0.99	1
7	0.96	0.99	0.98	0.99	0.98	0.97	0.99	0.98	0.97	0.99	0.98	0.98	0.99
8	0.97	0.99	0.99	1	0.98	0.98	0.99	0.98	0.98	0.99	0.98	0.99	0.99
9	0.99	1	1	1	1	1.01	1.01	1	1.01	1.01	1	1.01	1.02
10	0.99	1	1	1	1	1.01	1.01	0.99	1.02	1.01	1	1.01	1.03
11	1.00	1	1	1	1	1	1	1	1	1	1	1	1.01
12	0.99	1.01	1.01	1.01	1	1.01	1.01	1	1.03	1.02	1	1.01	1.03
13	1.00	1	1	1	1	1.01	1.01	1	1.02	1.01	1	1.01	1.02
14	0.98	0.99	0.99	0.99	0.99	1	1	0.99	1.02	1.01	0.99	1	1.02
15	0.97	0.99	0.99	0.99	0.99	1	1	0.99	1.02	1.01	0.99	1	1.02
16	0.98	1	1	1	0.99	1.01	1.01	0.99	1.01	1.01	0.99	1	1.02
17	0.98	1	0.99	0.99	0.99	1	1	0.99	1.01	1	0.99	1	1.02
18	0.97	0.98	0.98	0.98	0.99	0.99	0.99	0.98	1	1.01	0.98	0.99	1.01
19	0.97	0.98	0.98	0.98	0.99	0.99	0.99	0.97	1	1.02	0.98	0.99	1.01
20	0.97	0.99	0.98	0.98	0.99	0.99	0.99	0.98	1	1.02	0.98	0.99	1.01
21	0.97	1	0.98	0.98	0.98	1	1	0.98	1.01	1	0.98	0.99	1.03
22	0.98	1	0.99	0.99	0.99	1	1	0.99	1.01	1	0.99	1.01	1.02
23	0.97	0.99	0.98	0.98	0.98	1	1	0.98	1.01	1	0.98	0.99	1.03
24	0.97	0.99	0.98	0.98	0.98	0.99	0.99	0.98	1	0.99	0.98	0.99	1.02
25	0.97	0.99	0.98	0.99	0.98	0.99	0.99	0.98	0.99	0.99	0.98	0.99	1.01
26	0.95	0.97	0.97	0.97	0.96	0.97	0.97	0.96	0.98	0.97	0.96	0.97	0.99
27	0.98	1	1	1	0.99	1	1	0.99	1	1	0.99	1	1.01
28	0.97	0.99	0.99	0.99	0.98	0.98	0.99	0.98	0.98	0.99	0.98	0.99	1
29	0.96	0.98	0.98	0.98	0.97	0.98	0.98	0.97	0.98	0.98	0.98	0.98	1
30	0.95	0.97	0.97	0.97	0.96	0.97	0.97	0.96	0.97	0.97	0.98	0.97	1

V. CONCLUSION

In perspective of consistently expanding load demand in the power sector, DG is playing an extremely indispensable role to enhance the system performance by diminishing the real power loss and enhancing the voltage profile. Optimal size and position of DG are very important in the utilization of DG for loss minimization and voltage profile enhancement in electric power system. Inappropriate position of DG in the system process will prompt the negative impact on system task. This paper presents population based heuristic methods i.e. GA and ACO algorithms are used to put the optimal sizing of DG at suitable position. To approve the proposed technique, IEEE30-bus system is tested and the results obtained are compared. The results are tabulated and the average voltage profile enhancement is indicated graphically and tabulated. Reduction in active power losses and enhancement in voltage profile can be noticed. The results demonstrated that the implementation of DG in ACO is exceedingly viable in reduction total losses of real power and voltage profile enhancement compared with GA.

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